THERMODYNAMICS AND FREE VOLUME OF VARIOUS ALKALI HALIDES IN AQUEOUS D-MANNITOL SOLUTION

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ABSTRACT

Ultrasonic, density and viscometric investigations have been conducted on several alkali halides in 0.4 M aqueous D-mannitol solution at four different temperatures: 25, 30, 35 and 40°C. Free volumes, internal pressures, ionic viscosity coefficients, and hydration numbers have been calculated. Activation parameters of viscous flow were also calculated and all these properties were discussed in terms of structure-making or -breaking properties of electrolytes in aqueous D-mannitol solutions. Results show that in addition to viscometric properties, the temperature dependency of free volumes and internal pressures is found to be a powerful tool in elucidating the structure-making or -breaking properties of the electrolyte solutions.

INTRODUCTION

This paper continues our investigation of the physico-chemical properties of aqueous ternary systems of alkali metal halides [l-3]. The effects of sugars and polyols on the solvent properties of water and the interactions of such solutes with electrolytes and non-electrolytes is of biological and thermodynamic importance. In recent years, active interest has been shown in solute-solvent and solute-solute interactions, which were determined by the chemical structure of solute and solvent molecules. Ultrasonic studies are mostly limited in obtaining hydration numbers [4-61. However, recently, it is shown that ultrasonic velocity measurements, along with viscosity and density values, can be used to calculate important factors such as free volumes (V_t) and internal pressures (Π) [7]. Free volume is a fundamental property to be considered when explaining the variation in physico-chemical properties of liquid mixtures and aqueous electrolyte solutions [8,9].

In the present communication we report the results of ultrasonic velocity and density measurements of LiCl, CSCl, RbCl, sodium and potassium

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halides in aqueous D-mannitol solutions. Viscosity measurements were carried out on aqueous D-mannitol solutions of lithium, rubidium and cesium chlorides at four different temperatures. Using our experimental data along with the viscosity measurements of Vishnu and Misra [10], the free volume and internal pressure of various alkali metal halides in aqueous D-mannitol have been calculated at four different temperatures. Viscosity data were analyzed in terms of different viscosity equations to obtain information about ionic interactions prevalent at such high concentrations of electrolytes. Various thermodynamic parameters of viscous flow were also determined.

EXPERIMENTAL

Analytical reagent grade samples of alkali metal halides and D-mannitol, obtained from B.D.H. or Merck, were employed for the present work, and were used without further purification. All solutions were prepared by molar basis in nanopure water (sp. conductivity $\approx 8 \times 10^{-7}$ mhos). A 0.4 M pmannitol solution was used as a stock solution. Viscosity and density, and ultrasonic velocity measurements were obtained by the methods and with the apparatus described previously [1,2].

RESULTS AND DISCUSSION

It has been shown that the viscosity *B* coefficient is a valuable tool in understanding the structure-making (SM) or structure-breaking (SB) properties of solute molecules [11,12]. Viscosity *B* coefficients were obtained by three different procedures. The Jones-Dole equation [13], modified for higher concentration

$$
\eta_{\text{rel}} = 1 + BC \tag{1}
$$

was used to calculate *B* values from the relative viscosity data for all electrolyte solutions. *B* values were obtained employing the least-squares method. Viscosity data in the entire concentration range were fitted into the Goldsack-Franchetto equation [14]

$$
\ln[\eta_{\text{rel}}(1+XV)] = XE \tag{2}
$$

where E and V are parameters characteristic of the electrolytes and X is the mole fraction of the electrolyte in solution. E and V were obtained by solving eqn. (2) by a non-linear least-squares method using an HP 3000 computer. A typical fit of the equation for the chlorides of an alkali metal is presented in Fig. 1. The approximate values for *B* coefficients were obtained using the relation

$$
B = (E - V) / 55.51
$$
 (3)

Vishnu and Misra [10] have calculated *B* coefficients using Breslau and Miller's equation [15] for sodium and potassium halides

$$
V_{\rm e} = \frac{-2.5C + \left[(2.5C)^2 - 40.20C^2 (1 - \eta_{\rm rel}) \right]^{1/2}}{20.10C^2}
$$
(4)

and the average \overline{V}_e values thus obtained were fitted into the following equation

$$
B = 2.90\overline{V}e - 0.018\tag{5}
$$

for 1 : 1 electrolytes. *B* coefficients for lithium, rubidium and cesium chloride in 0.4 M D-mannitol solution were also calculated using the Breslau-Miller equation. All these values are presented in Table 1. *B* coefficients obtained for Na and K halides by Vishnu and Misra are also included in the table for comparison. The values of *B* coefficients obtained by the three different procedures do not agree very well, although they are of the same order of magnitude. Since different approximations were involved in the derivation of these equations, the observed differences in the values of *B* coefficients is not

Fig. 1. Test for eqn. (2).

946 3.16 2.16 2.16 0.098 38.96 38.96 38.94 5.596 4.80 5.33 5.35 5.33 5.33 5.33 5.33 5.33 5.46
Na K+ 5.93 0.0040 1.60 - 0.654 0.0047 1.88 - 0.61 0.0067 2.70 -0.49 0.0120 4.80 -0.17 $Rb+8.17$ - 0.0256 - 0.0256 - 0.0256 - 0.0196 - 0.0196 - 0.0196 - 0.0196 - 0.0064 - 0.0064 - 0.085 r.1.14 - 12.16 - 12.16 - 12.16 - 12.16 - 12.40201 - 12.40201 - 12.40201 - 12.40001 - 12.17 - 12.17 - 12.17 - 1 cl- 14.9 0.0000 1.981" 2.02 0.0001 0.00400 1.602 0.02 0.021 0.021 0.0000 1.891 0.021 0.0120 0.0120 0.0120 0.01 [19] 1920 - 1920 - 101 + 1920 - 12.56 - 12.56 - 12.47 - 12.47 - 12.6701 - 12.47 - 12.601 - 12.47 - 1 I- 25.30 - 25.30 - 27.20 - 27.20 - 27.4000 - 27.4000 - 27.48 - 0.04900 - 0.04900 - 0.04900 - 0.04900 - 0.0490

^a Values of B_+ in 1 mol⁻¹ and V_+ in cm³ mol⁻ H

TABLE₁

unexpected. Also, for eqns. (2) and (4) , the entire concentration range was utilized in the calculation of *B* coefficients. This could explain the difference in the trend of dependency of *B* values on temperature.

It has been shown [16] that the *B* coefficient may be considered as being formed by two contributions: one positive and one negative. The former comes from the tendency of the ions to attract the solvent molecules around it centro-symmetrically, while the latter stems from the fact that the structure of the solvent itself goes against this tendency, so that these two opposing influences can cause breakdown in the solvent structure beyond the first solvation shell.

Generally, the positive contribution prevails over the negative one, producing an increase in the viscosity of the solution with respect to that of the solvent. Only for solvents with extended three-dimensional structure, due to hydrogen bonds [17,18], does the negative contribution dominate for ions with low charge density, with negative B-values and a relative decrease in viscosity of the solution with respect to that of the solvent can be found. Following the above lines, one can discusss the variation of *B* coefficients in terms of viscosity effects. In a given series of alkali metal halides, e.g., chlorides, the charge density decreases in the order: Li^+ > Na⁺ > K⁺ > Rb⁺ $> CS^{+}$ and one can expect that B-values vary in the order LiCl $> NaCl$ $KCl > RbCl > CSCl$.

In order to distinguish the effect each single ion has in an aqueous 0.4 M D-mannitol solution, viscosity B-coefficient values were split into ionic contributions on the hypothesis that $B(K^+) = B(Cl^-) = B(KCl)/2$ as already reported [17]. B_+ values calculated according to the procedures of Kaminsky [17] are presented in Table 2. According to Gurney [19] dB_+/dT is either negative or near zero for structure-making ions and positive for structure-breaking ions. Examination of Table 2 reveals that $Li⁺$ and Na⁺ are definitely structure-making ions and all the other ions are structurebreaking. Positive $d B₊/dT$ values for anions could be due to the interaction of the ion with water molecules through hydrogen bonding. Slightly positive values of $d B_{+}/dT$ for Na⁺ ions initially may be due to carbohydrate-salt interactions involving the hydroxyl groups of D-mannitol and the ions [20].

Using ionic B_{\pm} values and assuming that the ions behave like a rigid sphere, one can calculate the ionic molar volumes of ions (V_+) according to Einstein's equation [21]

$$
B_{\pm} = 2.5\overline{V}_{\pm} \tag{6}
$$

where 2.5 is the shape factor for a sphere. Hydration numbers (N_B) of ions can be obtained from the equation

$$
\overline{V}_{\pm} = \overline{V}_{\text{ion}}^0 + N_{\text{B}} \overline{V}_{\text{s}}^0 \tag{7}
$$

where V_{ion}^{0} is the free ionic volume calculated from the equation $V_{ion}^{0} = 2.52r^{3}$ (r = ionic radius) and V_s^0 is the molar volume of water equal to 6.62 cm³

mol⁻¹. The values of N_B are presented in Table 2. According to Millero [22] and Curthoys and Mathieson [23] positive hydration numbers and negative $dN_{\rm B}/dT$ and dV_{\perp}/dT are characteristics of structure-making ions, whereas structure-breaking ions normally have negative hydration numbers and positive dN_B/dT and dV_+/dT . One can conclude from the examination of Table 2, that Li^+ and $N\overline{a}^+$ ions are structure-makers and K^+ , Rb^+ , Cs^+ , Cl^- , Br^- and I^- ions are structure-breakers in aqueous 0.4 M D-mannitol solutions.

According to Krestov [24], depending on the sign of the charge, a linear relationship exists between hydration number and entropy change in aqueous electrolyte solutions with ionic radius. When N_B is plotted against ionic radii or B_{+} we observed different linear relationships for positive and negative ions (Figs. 2 and 3).

This supports the idea [25,26] that $Li⁺$ and $Na⁺$ are electrostrictive structure-making ions with positive ionic volumes and hydration numbers, whereas K^+ , Rb^+ , Cs^+ , Cl^- , Br^- and I^- are structure-breaking ions with negative ionic volumes and hydration numbers. Probably the structurebreaking ions in solution disrupt the water structure by pushing water

Fig. 2. Plot of hydration number versus Pauling's ionic radii for alkali and halide ions in aqueous D-mannitol solution at **25°C.**

molecules apart in both primary and secondary hydration spheres. From the magnitude of hydration numbers, one can conclude that the structure-breaking ability of various ions in aqueous D-mannitol solution at 298 K is in the order: $I^- > Br^- > Cs^+ > Rb^+ > Cl^- > K^+ > Na^+ > Li^+.$

From the variation of viscosity with temperature, values of thermodynamic activation parameters of viscous flow were calculated [27]. The values are presented in Tables 3-5. From the dependency of thermodynamic parameters of viscous flow (ΔH^* , ΔS^* and ΔG^*) on concentration, one can divide the results into three types. In structure-making electrolytes, like LiCl and NaCl, the ΔH^* of viscous flow remains constant with an increase in concentration of the electrolyte within the experimental error, ΔS^* decreases and ΔG^* increases slightly. An increase in electrolyte concentration in these cases leads to an increased order in the activated state which thus becomes less favourable, compared to the unactivated state in aqueous D-mannitol solutions.

For structure-breakers, like CSCI, RbCl and KI, the ΔH^* and ΔS^* values decrease with an increase in concentration of the electrolytes, and ΔG^* remains constant. One can conclude that for structure-breakers, the activated

Fig. 3. Plot of hydration number versus ionic B coefficients for various alkali and halide ions in aqueous D-mannitol solution at 25°C.

 1.500 15.77 ± 0.49 19.30 ± 1.6 2.000 15.29 \pm 0.38 17.59 \pm 1 2.500 14.87 ± 0.34 16.07 ± 1.1 3.000 14.41 ± 0.44 14.39 ± 1.4

 15.77 ± 0.49 15.29 ± 0.38 14.87 ± 0.34

1.500

 17.59 ± 1.2 19.30 ± 1.6

 14.39 ± 1.4 16.07 ± 1.1

 14.41 ± 0.44

2.000
2.500
3.000

 10.02 ± 0.68 10.25 ± 0.53 10.08 ± 0.47 10.12 ± 0.61

 10.02 ± 0.68 10.25 ± 0.53 10.08 ± 0.47 10.12 ± 0.61

 15.45 ± 0.27 14.87 ± 0.29 14.43 ± 0.26 14.07 ± 0.26

 14.87 ± 0.29 15.45 ± 0.27

 14.43 ± 0.26 14.07 ± 0.26

 18.46 ± 0.88 16.39 ± 0.9 14.86 ± 0.85 13.45 ± 0.85

 18.46 ± 0.88 16.39 ± 0.95

 9.95 ± 0.37 9.98 ± 0.40 10.00 ± 0.3 10.06 ± 0.36

 9.98 ± 0.40 9.95 ± 0.37

 15.61 ± 0.29 14.99 ± 0.5 14.16 ± 0.54 13.66 ± 0.4

 14.99 ± 0.50 15.61 ± 0.29

 14.16 ± 0.54 13.66 ± 0.43

 10.00 ± 0.36 10.06 ± 0.36

 14.86 ± 0.85
13.45 \pm 0.85

 18.92 ± 0.95 16.76 ± 1.6 13.89 ± 1.8 12.01 ± 1.4

 18.92 ± 0.95 16.76 ± 1.6

 9.97 ± 0.43 0.70 ± 0.70 10.02 ± 0.75 10.68 ± 0.59

 $0.01 + 0.43$
0.9 ± 0.70

 10.68 ± 0.59 10.02 ± 0.75

 12.01 ± 1.4

 $\ddot{}$

164

TABLE 5 TABLE 5

Thermodynamic properties of viscous flow of electrolytes in 0.4 M aqueous p-mannitol solution Thermodynamic properties of viscous flow of electrolytes in 0.4 M aqueous D-mannitol solution

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state becomes more orderly and the energy required to break the bonds in the activated state decreases with an increase in concentration.

For the rest of the electrolytes the observed behaviour falls in between the above two cases. In these cases the structure-breaking ability of the anions dominates at higher concentration. ΔH^* and ΔS^* of viscous flow decrease with an increase in electrolyte concentration and the dependency of ΔG^* on concentration varies from Cl^- to I^- . For the structure-breaking electrolytes, ΔG^* is independent of electrolyte concentration and it could be attributed to the fact that the effect of ions in this group is relatively non-specific, a response which is expected from a common disrupting force on bulk water $[28]$.

The limiting values of activation parameters at infinite dilution of the electrolytes were obtained according to the procedures of Feakins et al. [29] and are presented in Table 6. According to these authors, the chemical potential change ($\Delta \mu_2^{0\#}$) is greater than that of pure solvent ($\Delta \mu_1^{0\#}$) for net structure-makers. From the data of Table 6, one can conclude that LiCl, KC1 and sodium halides are acting as structure-makers and the remaining electrolytes as structure-breakers at infinite dilution. From the dependency of $\Delta \mu_2^{0\#}$ on temperature, $\Delta S_2^{0\#}$ values and $\Delta H_2^{0\#}$ values were computed. Except for lithium ions the values of $T\Delta S_2^{0*}$ and ΔH_2^{0*} are negative, indicating that the formation of the activated complex is associated with bond making and an increase in order. For the lithium ions the transition is accompanied by bond breaking and a decrease in order. This suggests that the slip-plane is somewhere in the region of centro-symmetric order for lithium ions and in the disordered region for the remaining ions in aqueous D-mannitol solutions. A plot of $\Delta H_2^{0\#}$ against $T\Delta S_2^{0\#}$ indicates a linear relationship between these two parameters (Fig. 4) and the linearity depended on the ability of structure-making or -breaking properties of the ions.

Free volumes at all concentrations and temperatures were calculated using

^a Values in kJ mol⁻¹. $\Delta \mu_1^{0\#} = 9.80$ kJ mol⁻¹.

TABLE 6

the following formula [7]

$$
V_{\rm f} = \left(\,\overline{M}U/K\,\eta\,\right)^{3/2} \tag{8}
$$

where \overline{M} is the average molecular mass, U is the ultrasound velocity, η is the viscosity of the solution and K is a constant equal to 4.28×10^5 .

Internal pressures (Π) were calculated from the following equation [7]

$$
\Pi = bRT/V_{\rm m}^{2/3}V_{\rm f}^{1/3} \tag{9}
$$

where b is the packing factor in liquids (equal to 2 for cubic packing), and V_m is the molar volume of the media. Computed values are presented in Tables 7-14. Representative diagrams of free volumes against concentration at four different temperatures are presented in Figs. 5 and 6. Adiabatic compressibilities were also calculated and are included in the tables. Examination of Tables 7-14 indicates that the free volume dependency on concentration of the electrolyte depends on the type of the electrolytes. For net structure-makers like sodium and lithium chlorides, the free volume decreases with an increase in concentration of the electrolyte at all four temperatures. One can conclude that the high charge density of Li^+ and $Na⁺$ dominate the structure-breaking properties of the $Cl⁻$ ions in these electrolytes, resulting in the ordering of the solution and a decrease in free

Fig. 4. The relationship between ΔH_2^0 [#] and $T\Delta S_2^0$ [#] at 25°C.

volume. For all other electrolytes the structure-breaking properties of the anions dominate, resulting in an increase in free volume with an increase in concentration of the electrolytes. Similar behaviour is observed in the case of alkali metal halides in aqueous dimethyl formamide, aqueous urea and aqueous xylose systems (refs. 8, 2 and 3, respectively).

Internal pressure values show that, except for lithium and sodium chlorides, the values decrease with an increase in concentration at all temperatures. In a given series, internal-pressure values vary in the order: $Li^{+} > Na^{+}$ $> K^+ > Cs^+$ and $Cl^- > Br^- > I^-$. Higher values of internal pressure can be attributed to the electrostriction of the ions in solution. Adiabatic compressibility values decrease in all cases with an increase in concentration at all temperatures.

3.000 1690.1 3.23 1.627 28515

TABLE 7

LiCl system

TABLE 9

NaBr system

TABLE 10		

NaI system

TABLE 11

KC1 system

KBr system

TABLE 13

KI system

CsCl system

Fig. 5. Plot of V_f against molarity of NaCl in aqueous D-mannitol solution.

Fig. 6. Plot of V_f against molarity of KI in aqueous D-mannitol solution.

In conclusion, thermodynamic activation parameters of viscous flow, B coefficients, hydration numbers and their dependency on temperature are found to be very valuable in differentiating the structure-making and -breaking properties of the electrolytes in solution. Also, by coupling the viscosity values with ultrasonic velocity measurements, one can obtain two valuable parameters, namely free volume and internal pressure. It is found that the dependency of these parameters on concentration further throws light in terms of structure-making or -breaking properties of the electrolytes in solution.

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